

The Model of Compound Rod in Designing of Adhesive And adhesive-Mechanical Joints

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The capabilities of calculation methods for the design of adhesive and adhesive-mechanical joints are regarded, based on the model of the compound rod. Recommendations on estimation of the impact of number of structural factors and parameters on the load of the connecting node of layered construction.

Key words: Compound rod, Adhesive-mechanical joint, Load of connecting node, Connecting node of layered construction.

For the rational design of compounds it is necessary to have three main complexes of calculation methods to determine the load of the compound elements:

- a) general methods of compounds' calculating, based on the developed mathematical models to identify the determinant geometrical parameters and effort in power points, seams, adhesive interlayer, etc.;
- b) a set of ways to assess the impact on the joints' carrying capacity under static and cyclic load of the technological factors;
- c) methods of analysis of local strength on the weakened cross sections and forecasting of defects' development in the area of stress concentrators.

In design calculations of different types

of joints implemented in practice, complexes of calculation methods (except the first one), which are listed above are practically unused. Compounds' design is generally implemented by nominal shear or crushing stresses of fastener elements. The values of allowable stresses are taken on the basis of past operating experience of similar products in the relevant branches of machine industry (Belous and Khvatan, 1979).

Thus, in a typical calculation method of the strength of the adhesive joints, made of duralumin alloys (OS 92-0009-67) the strength of adhesive joint with shear τ_a and uniform separation s_a is calculated by the formulas:

$$\tau_a = F_b/A; s_a = F_b/A \quad \dots(1)$$

where

F_b – breaking load and A – adhesive area.

The strength of the adhesive joint with ununiformed break is determined by the test of patterns, which are firmly fixed plates, glued together with thin metal strips, separated from the base in a direction, perpendicular to the plane of gluing:

$$q_a = F_b/b \quad \dots(2)$$

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where b – glued layer width, q – breaking force per width unit. For flexible glued elements the strength within the separation of one from the other is determined.

The check of the strength of adhesive joints of metals is produced according to the following relations:

in shear – $(\tau_a/\tau)(\sigma_y/\sigma_s) \geq [n]$;

in uniform separation – $(\sigma_a/\sigma)(\sigma_y/\sigma_s) \geq [n]$;

in ununiformed separation – $(q_a/q)(s_y/s_s) \geq [n]$.

where σ , q – averaged operating stresses and efforts per joint width unit; σ_y , σ_s – yield strength and the strength of the connected parts respectively; $[n]$ – allowable strength factor, accepted for the main structure.

In the case of cyclic loading of adhesive joints of metal structural elements it is considered, as a rule, that the limit of their fatigue is about 10% of the static strength. If adhesive joint is exposed to corrosive environment, the value of the fatigue limit is reduced to a greater extent (two-component adhesives for the cold curing – up to 50%).

Low-cycle fatigue limit of metal adhesive joints is taken about 30% of the static strength limit. Regulatory strength factor should be selected at least.

This (traditional) method of determining the geometric parameters of adhesive joints, used with some additional restrictions, is based on experience in metallic structural components using high-strength hot curing adhesives, which confirms that the service life of these joints is from 5 to 10 years.

Recently, as a basis for modeling of the joints' mechanics finite element method is widely used (Galager, 1984; Semin, 1989; Pizzi and Mittal, 2003; Composite materials handbook, 2002). The algorithm of the method allows conducting the study of constructions within the most general boundary conditions and external loads, it has sufficient flexibility and high precision, allows us to analyze the constructions of complex configurations, characterized by great flexibility in presenting complex areas and boundary conditions. In this case, the real picture or process can be described in more complex functions than taken as a basis in finite elements, gradients of the studied values may be in conflict with the separation accuracy, implemented in practice, modeling of the boundary area by the set of points

in contact tasks is not always justified, representation of time processes is integrated with unjustified labor intensity.

Therefore, for the purposes of development of practical recommendations for the design of joints do not lose their actuality of mathematical models and calculations of adhesive adhesive-mechanical joints, based on the study of the mechanics of multi-layer compound rod (Sparrow and Sirotkin, 1985; Sazhin, 1964; Semin, 1982; Semin and Skoriy, 1976). It is assumed that the stresses and deformations of layers are defined by the materials' resistance formulas, and connecting elements (adhesive layer, rivets, welding, ..) transfer the load from one layer to another and work primarily in shear and break.

In the calculations of the metal adhesive joints, within determining of the shear modulus, elastic modulus and Poisson's ratio G , E , in the adhesive layer it must be taken into account that it is structurally anisotropic. In this case, the adhesive layer is glued between two rigid elements, and on the boundary "adhesive-metal" adhesive forces under load of the joint restrict deformation of adhesive material. These limitations have significantly greater influence on longitudinal deformation than angular. Therefore, the longitudinal elastic modulus of the adhesive layer increases considerably (2... 2.5 times) than the shear modulus (40...60%), compared with the corresponding values of the elastic characteristics of the cured from adhesive casting of polymer bonding agent.

Restriction of deformation of the polymer bonding agent affects the Poisson's ratio m as well. Poisson's coefficient value of the adhesive layer is reduced as compared with the value of the cured adhesive casting m_a . Furthermore, m coefficient depends on the kind and deformation of the joint. On the thickness of the adhesive layer m coefficient changes from Poisson's coefficient value of the glued material at the boundary "adhesive-metal" to a certain value in the center of the adhesive layer, which depends on the type of deformation, but does not exceed the coefficient of the cured adhesive casting.

As an example of one of the tested complexes of calculation methods let us consider the calculations of adhesive joints and adhesive-mechanical joints taking into the consideration the

bevel edges, nonlinear elastic characteristics of the binder and the dynamic nature of loading (Vorobey and Sirotkin, 1985; Sazhin, 1964; Semin, 1982; Semin and Skoriy, 1976; Semin and Turchinsky, 1985), allowing to conduct both a general analysis of the workload of the connecting node, depending on the design parameters and evaluate the nature of the stress' concentration in the area of mechanical fasteners, to forecast the durability.

When taking into account the bevel edge, the stress-deformed state of the joints is described by a system of ordinary differential equations with variable coefficients (Semin and Skoriy, 1976). Typical diagrams of normal and shear stresses along the gluing, reduced to dimensionless form, shown in Figure 1. The solution has been conducted by the numerical method of orthogonal sweep.

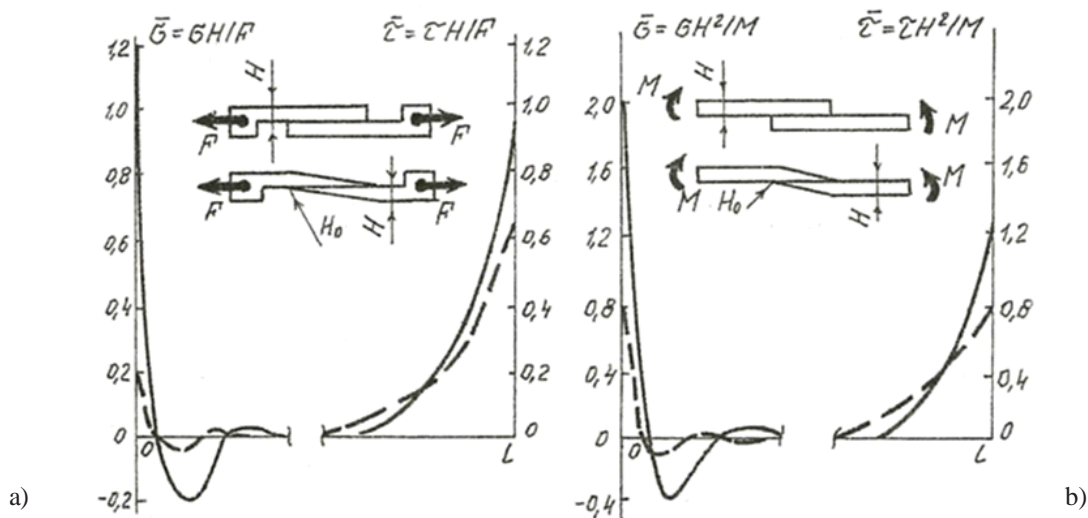


Fig. 1. Stresses' distribution in the joints of the "simple overlapping" (-) and "overlapping with beveled edges" (- -) under tension (a) and bending (b): $E_1 = E_2 = 7 \times 10^4$ MPa; $\mu = 3 \times 10^3$ MPa; $d = 0.2$ mm; $l = 50$ mm; $H_0/H = 0.1$, where H_0 —minimal plate width at the joint end

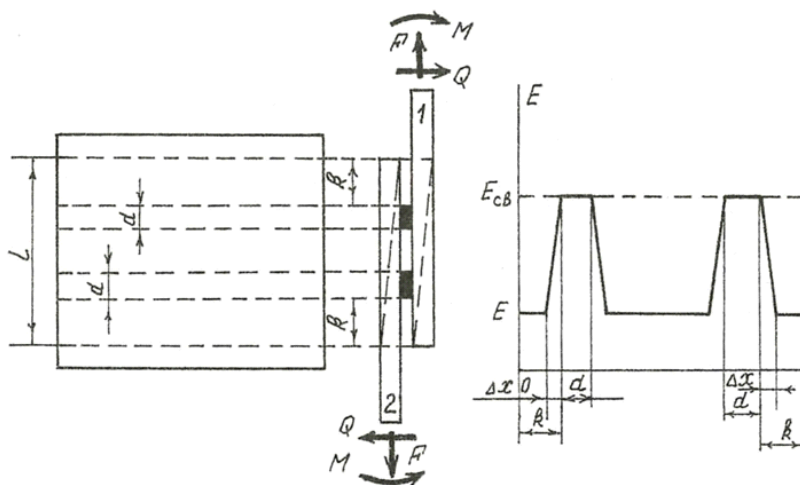


Fig. 2. Design model of the combined adhesive-welding joint of the "simple overlapping" and "overlapping with beveled edges" (- -).

The line of action of the tensile load lies along the joint axis, i.e. it is not required to take into account the distortion of the configuration under the load of the joint. At the edges of the calculated adhesive node parts (apart from the tensile force F) the bending torque takes place $M = FH/2$, where H – the thickness of the joined sheets. Two weld seams of 2 mm wide, performing the role of mechanical fasteners are placed at the same distance k from the edges of the joint (Figure 2) (Ionov and Kutynov 1979, Cagle, 1971; Kutynov, 1979; Pescherova and Kozlov, 2007).

The hypothesis is accepted, according to which the change of stiffness of the connecting layer at the places of the transition from the adhesive and mechanical fasteners and back is linear in a sufficiently small interval $DE = 5$ mm with the lengths of the adhesive-mechanical joint $l = 50$ mm. Modulus of elasticity of the adhesive layer is assumed to be $E = 3 \times 10^3$ MPa. The performed calculations are conducted for practically used thicknesses of the adhesive layer of $d = 0.2$ mm in the design. The modulus of elasticity of the material of mechanical fasteners is accepted as $E_b = 7 \times 10^4$ MPa. Joined sheets are considered as made of the same material with an elastic modulus $E_1 = E_2 = 7 \times 10^4$ MPa.

When the location of the welding seams is at the very edges of the joint ($k=0$), a sharp increase of stresses concentration, compared with purely adhesive joint, which falls within the material of the welded seam. The adhesive layer is located between two welding seams is practically not loaded, providing a monolithic work of the compound construction.

Location of welding seams at a small distance from the edges of the joint of the “simple overlap” type ($k = 2.5$ mm) leads to a greater load of the part of the polymer adhesive layer at the edges of the joint than in purely adhesive joint. At the same time on the tangent (shear) stresses such an arrangement of the welding seams has practically no effect, while the normal (break) stresses in the adhesive are increased significantly (Fig. 3). In joint with the beveled edges ($\gamma_0 = 0.1 H$, where H_0 – minimum sheet thickness at the junction area) within this location of the welding seams, the adhesive layer part, located at the edges of the joint is actually loaded in the same manner as in purely adhesive joint. In both cases, the weld material works in shear. In the second case the welding seams are loaded by

the break stresses significantly less (Designing, calculation and testing of composite materials' constructions, 1975).

Within further displacement of the welding seams to the middle of the joint ($k \approx 5$ mm) the load, falling within them is significantly reduced: the effort transfer from one of the joined sheets to another is carried out by a polymer adhesive layer at the edges of the joint. The polymer adhesive layer is loaded with almost the same extent as in a pure adhesive joint, wherein the adhesive layer in the middle of the node is not loaded. In such joints welding seams act as preventing mechanical reinforcements.

The main efficacy of the use of adhesive-mechanical joints in comparison with the use of other types of joints is achieved by the fact that the combined joints the basic part of the load is taken by the glue. As a result, the peaks of the stresses' concentration in the glued parts “smeared out”, that considerably increases the carrying capacity of the joints. Elements of the mechanical fasteners (bolts, rivets, welding seams) are used to improve the reliability of the connections, experiencing irregular (mostly break) loads. From this point of view, the use of adhesive-mechanical joints with beveled edges is more appropriate than the combined joints of “simple pad” type because

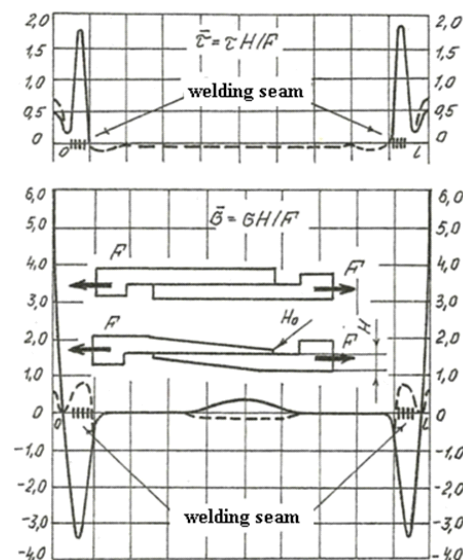


Fig. 3. Distribution of tangential normal stresses in the binding agent along the combined adhesive-welding joint (--- for the joint with the beveled edges)

the mechanical fasteners work more efficiently at the force transfer, and the adhesive layer experiences less break stresses. If mechanical fasteners are in the area of the transmission of forces, determined for the same purely adhesive joint, a significant increase in stress in the polymer adhesive bonding agent at the ends of the joint is absent and the load of the elements of the mechanical fasteners is increased (Khvatan, 1979; Tsarahov, 1980; Shvechkov and others, 1985).

The considered model of the joining of two sheets of pliable elastic layer is acceptable to analyze the strength of the joints, made on the basis of rigid high-strength structural adhesives. It can also be used to estimate the behavior of the adhesive structures with significant nonlinearity of deformation of the adhesive layers. In these cases, the smaller values of the elastic modules of the adhesive layers should be programmed in the calculations.

CONCLUSION

When designing the adhesive joint it is necessary to consider the following factors:

1. The stress distribution in a two-layer compound structure depends on the boundary conditions and parameters $D_1 = EH/E1d = EH/E2d = H_0/H$.
2. Bevel of the edges of the sheets due to the increase of suppleness by 60-70% reduces the stress of the break in the adhesive and has little effect on the shear stresses.
3. The parameters that characterize the mechanics of the transmission of the forces from one part to another. Within their small value of the transmission of the forces takes place throughout the joint (parameters close to 0.15). Increasing the parameters reduces the efforts' transmission zone and increases the concentration of stresses.

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