

A Metaphorical Scrutiny in Banishing Salt and Pepper Noise Using Time Domain and Frequency Domain Filters

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In this paper, an attempt is made to de-noise the image using isolation model and a comparison is made between the existing time domain and frequency domain filters based upon their performance analysis, and parametric estimations. An image gets corrupted by various noises during transmission through the channels. One of the noise types that include for image noising is salt and pepper noise. Salt and pepper noise is also known as Impulse noise. The main objective of filter is to remove the impulse noise without affecting the original image. The filters used for de-noising are of two domains, they are time or spatial domain and frequency domain. The time domain filters include mean, median, standard median filter and Decision Based Unsymmetrical Trimmed Median filter (DBUTM). The frequency domain includes the discrete wavelet transform (DWT) using shrinkage rule. The experiment result shows that the isolation algorithm provides better de-noising than the time domain filters and DWT.

Key words: DBUTM, DWT, frequency domain, Isolation, mean, median, and time domain.

An image gets affected by noisy pixels during the acquisition and transmission through various channels. The severity of noise in the image can be identified by the bit error values. The noise signals are classified into two main types based on the distribution of noisy pixels - (i) fixed- Valued noise (ii) random valued impulse noise [Dodda Shekar *et al*, 2011] [Chi-Yuan Lien *et al*]. The fixed-valued noise is also known as salt and pepper noise. In images that are corrupted by salt and pepper noise contains the corrupted pixel with maximum or minimum grey level [S.Esakkirajan *et al*, 2011]. The minimum gray level (0) is said to be as salt or white noise and the maximum gray level (255) is represented as pepper or black noise. The

denoising methods involved in salt and pepper noise are classified into two types (1) Low – complex methods and (2) High-complex methods [Venkatsubramanian Adhinarayanan *et al*, 2012]. The filtering methods [S.Karthikeyan *et al*, 2014] like mean, median and DBUTM belongs to low complexity technique and the methods like DWT, isolation are included in the High-complexity techniques.

Review on time domain filters

In [Dodda Shekar *et al*, 2011], the DBUTM for the removal of salt and pepper noise is proposed as a modified concept of decision based algorithm. It is a modified sheer algorithm and found to be more efficient than the median filter in edge preserving. In [K.Vasanth *et al*, 2012], the proposed Unsymmetrical Trimmed variants algorithm is found to be effective than the conventional existing algorithm and adaptive median filter till 30% of impulse noise. In

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[S.Esakkirajan *et al*, 2011]], a modified Decision based unsymmetrical algorithm is proposed which seems to have better PSNR and IEF compared to median filter, adaptive median filter, and decision based algorithm. In [Gajanand Gupta , 2011], a mathematical model for mean, median and improved median filter is designed for the corrupted lena image consisting of various noise types and noise levels using steady fixed window length size. In [M. Prema Kumar *et al*, 2011], a new concept of decision based IQA algorithm is used to remove salt and pepper noise from the image and concluded that this algorithm removes only corrupted pixels by the median value or by its neighboring pixels without disturbing the original image. As a result it de-noises effectively even at 90% noise level and preserves the edges without any loss up to 80% noise level. In [Vishal Gautam *et al*, 2012], an improved median filtering for the removal of salt and pepper noise is presented and compared with simple mean and median filter based on the PSNR Values and found that the improved algorithm preserves the integrity of edge and detailed image information. In [Gurmeet Kaur *et al*, 2013], a conclusion is made that the wavelet transform performance is better than the Gaussian, average, wiener, and median filter by comparing the parameters such as PSNR, RMSE, Entropy and correlation of the image. In [Sanjay Singh *et al*, 2012], the method of de-noising the salt and pepper noise by applying median filter and high pass filter is made and found that the median filter removes the noise and high pass filter preserves the edges. In [Slem saleh Al-amri *et al*, 2010], the de-noising of three types of noises such as salt and pepper noise, speckle noise, and Random Valued Impulse noise is studied using mean filter, adaptive wiener filter, Gaussian filter, Standard median filter and adaptive median filter and concluded that adaptive median filter is better to remove Salt and pepper noise and Standard median filter is good when noise level is less than 40%. In [T.K.Thivakaran *et al*, 2010], adaptive median filtering method is proposed in comparison with median filter and central weighted median filter to de-noise an image and found AMF provides better performance. In [32], an attempt is made to study the performance analysis between median filter and wiener filter. He found that wiener is better in denoising the speckle and Gaussian noise and median is better in

removing the salt and pepper noise than wiener.

Frequency domain filters

Wavelet Transform

Wavelet is based on the mathematical functions that involves in splitting data into various frequency components and then approach each component with a resolution matched to its scale. It provides better de-noising than the time domain filters by separating noisy signal from the image. The wavelet *also* provides better energy compaction than the previous filters. A wavelet transform is a representation of various wavelet functions. The de-noising is done by finding the threshold value for each part by using Shrinkage rules. The steps involved in this are

Step1: To decompose the corrupted image apply DWT

Step 2: Calculate the threshold value.

Step3: Apply soft threshold concept to the noisy coefficients.

Step 4: Apply inverse DWT.

In this each decomposed part is threshold by comparing it with the threshold value calculated Bayes Shrink. The variance is the important parameter in Bayes shrinkage calculation. It is calculated by summing the variance of the original pixel with the variance of noise applied on the image. The Bayes Shrink is calculated by using

$$\sigma_y^2 = \sigma_x^2 + \sigma^2 \quad ..(1)$$

σ_y^2 is the variance of noisy image.

σ_x^2 is the variance of original image.

σ^2 is the noise variance.

$$\sigma_y^2 = \{\sum b_m^2\}/M \quad ..(2)$$

Where b_m is the coefficient of wavelets and $m=1$.

M is the number of sub band coefficients.

$$\sigma_x^2 = \text{sqrt} [\max (\sigma_y^2 - \sigma^2, 0)] \quad ..(3)$$

$$\sigma = \text{median} [d(i, j)] / 0.6745R \quad ... (4)$$

$$\lambda = \sigma^2 / \sigma_x^2$$

The equation (1) provides the calculation of variance of a Bayer shrinkage and equation (2), (3) and (4) represents the formulae to calculate the variance of noisy pixel, original pixel and the variance of the noise added to the image. The Bayes Shrink is selected for its efficient in providing smoothening of reconstructed image.

Isolation algorithm

In general, the non –corrupted pixels in

the smooth region should be of nearer values or of slightly varying values. The corrupted pixel in a matrix of window size 3x3 can be determined by the distribution of larger different values with the surrounding pixels.

a	b	c
d	M(i,j)	e
f	g	h

A current pixel in a matrix can be determined by the smoothness of its surrounding pixels. In this algorithm, a noisy pixel can be considered as an isolation point. If the difference between the noisy pixel and its surrounding pixels are found to be large, then the following steps are to be followed.

Step1: Find the maxima and minima luminance values of a matrix.

Step2: Consider the first row as top half and the third row as bottom half in a 3x3 window.

Step3: Find the maximum and minimum value of top half and is represented by the α_{\max} and α_{\min} . The difference in luminance value is given by $\alpha_d = \alpha_{\max} - \alpha_{\min}$. Similarly, the maximum and minimum value of bottom half is given by the symbol β_{\max} and β_{\min} . The difference is given by $\beta_d = \beta_{\max} - \beta_{\min}$.

Step4: To find whether the surrounding pixels form a smooth region, compare the $\hat{\alpha}_d$ and $\hat{\beta}_d$ values with the Threshold value Th_1 .

Steps to find a noisy pixel

Step5: Consider a pixel P(i,j) and center pixel is represented by M(i,j).

Step6: Calculate $[M(i,j) - \alpha_{\max}]$ and $[M(i,j) - \alpha_{\min}]$. Then Calculate $[M(i,j) - \beta_{\max}]$ and $[M(i,j) - \beta_{\min}]$. The values obtained are compared with the threshold value Th_2 . If the values exceed the threshold value, then it is a noisy pixel.

Step 7: The edge in the current window is determined by the edge preserving method. In this, only eight different directions (D1 TO D8) in a window are considered to eliminate noisy pixel. The directions through the suspected noisy pixels are eliminated.

For example, if a, b, and c is a de-noised pixel and the remaining are noisy, then the directions through a,b, and c alone are considered to find the estimated value of a current pixel $P^{\wedge}(i,j)$. It is calculated using the formulae $(a+2xb+c)/4$.

Step 8: If an edge is considered, find the minimum

difference (Dmin) among the chosen directions.

Step 9: Then take the mean of the pixels which constitute the minimum direction.

Step 10: To preserve the edge of the image apply median to the estimated pixel $P^{\wedge}(i,j)$ and its surrounding four neighboring pixels.

RESULTS

The parameter that determines the image Quality is MSE, RMSE, PSNR etc.,

Mean Square Error: The MSE represents the cumulative squared error between the compressed and the original image, whereas PSNR represents a measure of the peak error. The lower the value of MSE represents the lower value of the error.

The MSE brings out the difference between the original image and the noisy image and averaging the difference with the product of the number of pixels used. The MSE value varies based upon the noise level applied to an image. It is given by the formulae

$$MSE = \frac{1}{MN} \sum_M \sum_N (x(i, j) - y(i, j))^2$$

Algorithm to calculate Mean Square Error:

Step1: Calculate the difference between the noisy pixel and original pixel.

Step2: Calculate the size of the matrix

Step3: Each of the pixels in the matrix has to be squared.

Step4: Calculate the sum of the matrix obtained in step3

Step5: Calculate the MSE by taking the ratio of value in Step4 to the value in Step2.

Step6: Calculate the RMSE by taking the square root of step 5.

Signal to Noise Ratio: The parameter that determines the image quality is given by PSNR values. The increase in PSNR values shows the increase in image quality. The expression for it is given by

$$PSNR = 10 \log \left(\frac{255^2}{MSE} \right)$$

Algorithm to calculate Peak Signal to Noise Ratio:

Step1: Calculate the difference between the noisy pixel and original pixel.

Step2: Calculate the size of the matrix

Step3: Each of the pixels in the matrix has to be squared.

Step4: Calculate the sum of the matrix obtained in step3

Step5: Calculate the MSE by taking the ratio of value in Step4 to the value in Step2.

Step6: Calculate the RMSE by taking the square root of step 5.

Step7: Calculate the PSNR by dividing 255 with RMSE. Then take log base 10 of that and multiply it with 10.

The Simulation is performed using Matlab version 7.10.0. The image used to study the performance of various de-noising methods is a standard baboon.jpg image.

The Table1 explains the analysis report MSE values of various filters on the image.

The RMSE of the filtered output images of various filters are given in Table 2.

The Table3 provides the most important parameter PSNR that determines the quality of an

image. The higher the PSNR value Higher the quality of an image. It is found to be high for the isolation algorithm.

The images shown below are an output of the removal of 50% salt and pepper noise from the Jpeg image. Only the d) wavelet image appeared to be in black and white image since it involves color to grey conversion. The image e) isolation image has better quality than the other filters.

The figure 1.a) represents an original baboon.jpeg image and the output image of mean, median and DBUTM filter is given in figure 1.b), c) and d) respectively. The figure 1.e) and f) gives the output of DWT and isolation method.

The Figure 2 explains the graphical representation of the above discussed filters by plotting noise density Vs PSNR value. The Red colored graph indicates the values of isolation method and is found to be higher than the other methods

Table 1. MSE values of different filters

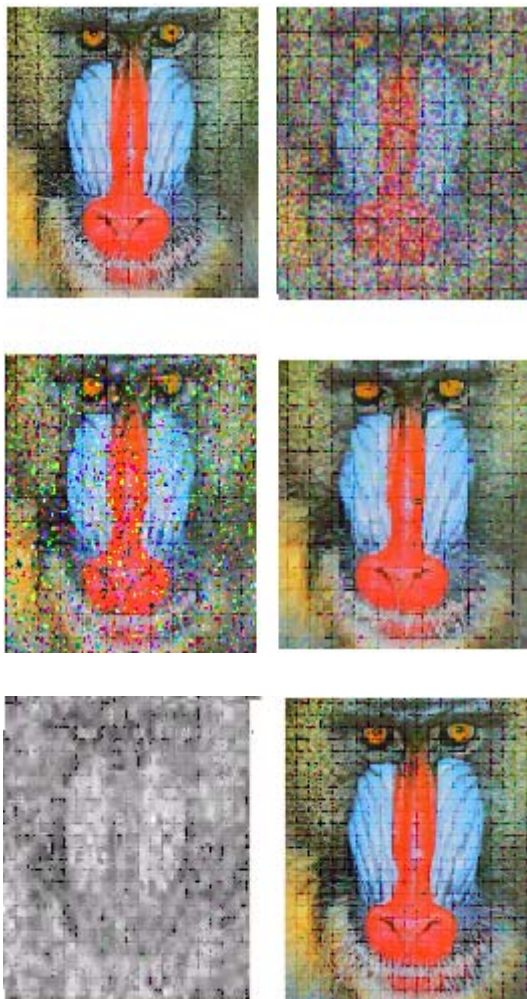
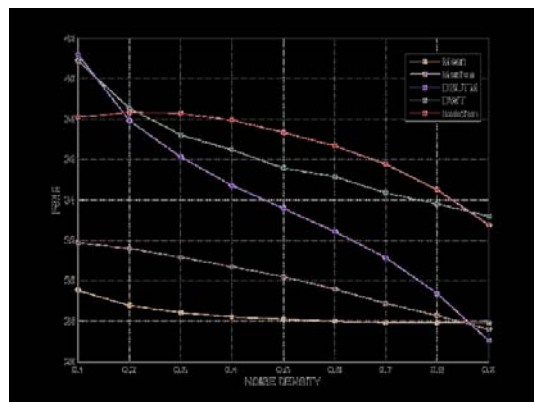
Noise Density In %	MSE				
	Mean	Median	Dbutm	Wavelet	Isolation
10	72.3966	42.4365	4.9279	21.2888	48.43
20	86.3031	45.2216	10.486	36.7029	41.60
30	93.5664	49.5127	15.847	49.7239	42.04
40	98.3936	54.9268	21.984	58.7196	44.77
50	100.976	62.3416	28.438	72.6914	50.19
60	103.691	72.1617	36.941	79.9328	56.93
70	105.395	82.9187	50.024	96.4967	68.06
80	105.733	96.8950	74.974	109.3794	86.86
90	106.322	112.272	128.51	128.5133	120.69

Table 2. RMSE values of various filters

Noise Density In %	RMSE				
	Mean	Median	Dbutm	Wavelet	Isolation
10	8.5086	6.4935	2.2198	4.6784	6.959
20	9.2899	6.7150	3.2383	6.0582	6.449
30	9.6729	7.0566	3.9808	7.0515	6.483
40	9.9193	7.4348	4.6888	7.6628	6.691
50	10.0486	7.8845	5.3327	8.5259	7.084
60	10.1828	8.4590	6.0779	8.9405	7.545
70	10.2662	9.1585	7.0728	9.8232	8.249
80	10.2826	9.8311	8.6587	10.4584	9.319
90	10.3112	10.6284	11.336	11.2166	10.985

Table 3. : PSNR values of different filters

Noise Density In %	PSNR IN DB				
	Mean	Median	Dbutm	Wavelet	Isolation
10	29.5383	31.8823	41.211	40.9537	38.1039
20	28.7827	31.5907	37.924	38.5485	38.3195
30	28.4364	31.1599	36.133	37.3461	38.2735
40	28.2250	30.7071	34.711	36.4976	37.9450
50	28.1163	30.1955	33.593	35.7408	37.3500
60	28.0072	29.5846	32.457	34.9580	36.6927
70	27.9397	28.8943	31.139	34.3276	35.7620
80	27.9319	28.2788	29.381	33.8421	34.4912
90	27.9064	27.6015	27.042	33.0945	32.7771

**Fig. 1.** The output images for 50% noise level**Fig. 2.** Plot for PSNR values of various filters

Based on the above analysis isolation method provides better performance than the DWT except for the noise levels 10% and 90%. The wavelet provides better PSNR VALUES than the mean, median and DBUTM. Also the PSNR values of Isolation method are found to be nearer to DWT. But the output image of DWT occurs blurred since the wavelet is applied only to the frequency component.

REFERENCES

1. Chih-Yuan Lien, Chien-Chuan Huang, Pei-Yin Chen, and Yi-Fan Lin, "An Efficient Denoising Architecture for Removal of Impulse Noise in Images", *IEEE TRANSACTIONS ON COMPUTERS*.
2. Dodda Shekar and Rangu Srikanth., "Removal of High Density Salt & Pepper Noise in Noisy Images Using Decision Based UnSymmetric Trimmed Median Filter (DBUTM)",

- International Journal of Computer Trends and Technology*-2011; **2**(1).
3. S. Esakkirajan, T. Veerakumar, Adabala N. Subramanyam, and C. H. PremChand "Removal of High Density Salt and Pepper Noise through Modified Decision Based Unsymmetric Trimmed Median Filter", *IEEE SIGNAL PROCESSING LETTERS*, 2011; **18**(5).
 4. Gajanand Gupta, "Algorithm for Image Processing Using Improved Median Filter and Comparison of Mean, Median and Improved Median Filter", *International Journal of Soft Computing and Engineering (IJSCE)*, ISSN: 2231-2307, 2011; **1**(5).
 5. Gurmeet Kaur and Jagroop Singh, "Performance Evaluation of various Image De-noising Techniques.", *Journal of Information and Computing Science*, 2013; **8**(1); 013-026.
 6. K.Vasanth, S.Karthik and Sindu Divakaran "Removal of Salt & Pepper Noise using Unsymmetrical Trimmed Variants as Detector", *European Journal of Scientific Research*, ISSN 1450-216X, 2012; **70**(3), pp. 468-478.
 7. M. Prema Kumar, V.Srinivasa Rao, and Dr.P.Rajesh Kumar, "Removal of High Density Noise in Digital Images using Decision based IQA Algorithm", *IJECT* **2**, SP-1, Dec. 2011.
 8. Sachin D Ruikar and Dharmpal D Doye, "Wavelet Based Image Denoising Technique", (*IJACSA*) *International Journal of Advanced Computer Science and Applications*, 2011; **2**(3).
 9. Sanjay Singh, Chauhan R.P.S, and Devendra Singh, "Comparative study of image enhancement using median and high pass filtering methods", *Journal of Information & Operations Management*; 2012, **3**(1), p96.
 10. Slem saleh Al-amri, Dr. N.V.Kalyankar and Dr.Kamitkar S.D,"A comparative study removing noise from remote sensing image." *IJCSI International Journal of Computer Science Issues*, 2010; **7**(1), No. 1.
 11. Suresh Kumar, Papendra Kumar, Manoj Gupta, Ashok Kumar Nagawat. "Performance Comparison of Median and Wiener Filter in Image De-noising", *International Journal of Computer Applications* 2010; (0975 – 8887) **12**(4).
 12. T.K.Thivakaran and Dr.R.M.Chandrasekaran, "Non-linear filter based image de-noising using AMF approach.", (*IJCSIS*) *International Journal of Computer Science and Information Security*, 2010; **7**(2).
 13. Venkatasubramanian Adhinarayanan, S.P.Sheebha, L. Sriraman, T. N. Prabakar, and G. Seetharaman, "A Modified algorithm for Removal of Salt and Pepper Noise in Color Images", *Third International Conference on Intelligent Systems Modelling and Simulation* - 2012.
 14. Vishal Gautam & Tarun Varma, "Reconstruction of Corrupted Image from Salt and Pepper Noise from Median Filter", *Undergraduate Academic Research Journal (UARJ)*, ISSN: 2278 – 1129, 2012; **1**(1).
 15. Vinod Kumar, Anil kumar and Pushpraj pal, "Image de-noising using hybrid filters", *International Journal of Data & Network Security* www.cirworld.com 2012; **1** (1).
 16. S.Karthikeyan, S.Shanmugapriya, S.Jayashri, Saravanan, "Sub-Head Transmission of Heterogenous data by Cloned agent to android mobile". *Research Journal of applied sciences Engineering and Technology*, 2014; **8**(1); pp.24-34, ISSN: 2040-7459; e-ISSN: 2040-7467